## ALM 2017

## 1. Interest rate analysis

Today is 1st January 2013. You find the following report on government bonds:

| Last trading date |  |  |
| :---: | :---: | :---: |
| 31.12 .2012 | Coupon rate <br> (annual coupons) | Bond yield <br> (annual compounding) |
| Bond maturity | $5,00 \%$ | $7,945607 \%$ |
| 31.12 .2013 | $5,00 \%$ | $7,616424 \%$ |
| 31.12 .2014 | $5,00 \%$ | $7,333579 \%$ |
| 31.12 .2015 | $5,00 \%$ | $7,091740 \%$ |
| 31.12 .2016 | $5,00 \%$ | $6,885408 \%$ |
| 31.12 .2017 | $5,00 \%$ | $6,709395 \%$ |
| 31.12 .2018 | $5,00 \%$ | $6,559044 \%$ |
| 31.12 .2019 | $5,00 \%$ | $6,430306 \%$ |
| 31.12 .2020 | $5,00 \%$ | $6,319723 \%$ |
| 31.12 .2021 | $5,00 \%$ | $6,224383 \%$ |
| 31.12 .2022 |  |  |

1.1 Determine the term structure of zero rates (the yield curve).
1.2 Determine forward rates that are consistent with the zero rates.
1.3 Produce a graph showing the zero rates and forward rates.
1.4 What does one call a yield curve that has a shape as this one?

Please state all interest rates with continuous compounding.

## 2. Liability funding

Today is still 1st January 2013. You want buy bonds to fund a 10 -year fixed annuity of $€ 1,000,000$ per year, starting 31.12.13.
2.1 Determine the portfolio of bonds that replicates the liability cash flow.
2.2 Determine the portfolio of bonds with maturity in 3-5-10 years that matches the present value, duration and convexity of the liability cash flow.

Please use continuously compounding interest rates in all calculations.

